

**II B. Tech II Semester Regular Examinations August - 2014**

**CONTROL SYSTEMS**

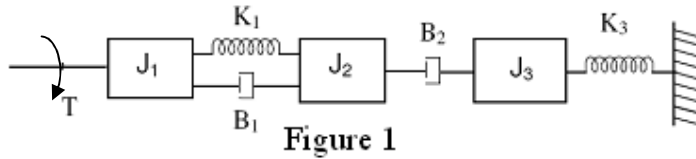
(Com. to EEE, ECE, EIE, ECC, AE)

Time: 3 hours

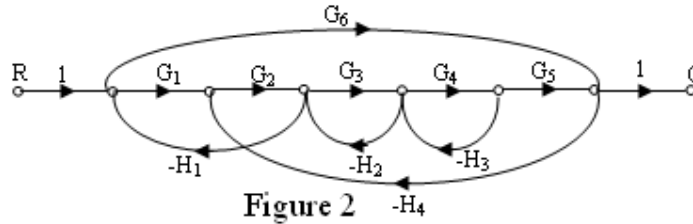
Max. Marks: 75

Answer any **FIVE** Questions  
All Questions carry **Equal** Marks

1. a) State essential differences by giving suitable examples and also highlight their merits and demerits for open loop and closed loop systems.
- b) Write the differential equations for the Mechanical rotational system shown in Figure 1. Draw the Torque-voltage and Torque-current electrical analogous circuits. (8M+7M)



2. a) Derive the transfer function of armature controlled dc servomotor.
- b) For the system illustrated by the signal flow graph shown in Figure 2, obtain the overall transfer function by means of Mason's formula. (7M+8M)



3. a) Illustrate the effects of proportional integral control on transient performance of feedback control systems.
- b) For a unity feedback system with open loop transfer function  $G(s) = \frac{50}{(1 + 0.1s)(1 + 2s)}$  determine position, velocity and acceleration error constants. (8M+7M)

4. a) Construct Routh array and determine the stability of the system represented by the characteristic equation,  $s^7 + 7s^6 + 20s^5 + 24s^4 + 24s^3 + 20s^2 + 20s + 15 = 0$ . Comment on the location of the roots of characteristic equation.

- b) Sketch the root locus plot of unity feedback system having open loop transfer function given by:  $G(s) = \frac{K(s+1.5)}{s(s+1)(s+5)}$ . (7M+8M)

5. The open loop transfer function of a unity feedback control system is given by:

$$G(s) = \frac{1000}{s(0.1s + 1)(0.001s + 1)}$$

Draw Bode plots and from these plots determine gain margin and phase margin. (15M)

6. For a unity feedback system having open loop transfer function given by

$$G(s) = \frac{K}{s(s+1)(s+2)}$$

Find the range of values of K for closed loop system stability using Nyquist criterion. (15M)

7. a) Draw electrical network configuration for phase-lead compensator and hence derive the transfer function for the same.

b) Explain the procedural steps to design a phase lag compensator using Bode analysis.

(7M+8M)

8. a) Explain about the concept of controllability and observability.

b) Check the controllability and observability of the system described by

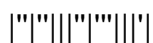
(7M+8M)

$$\dot{x} = Ax + Bu$$

$$y = Cx$$

With

$$A = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ 0 & -2 & -3 \end{bmatrix}, B = \begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix} \text{ and } C = [3 \quad 4 \quad 1]$$



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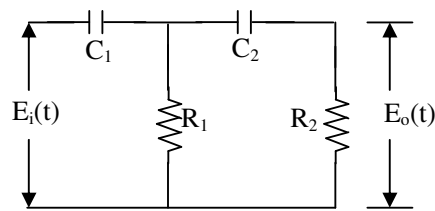
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1. a) Explain the necessity and effect of feedback in control systems?  
b) Determine the transfer function  $E_o(s)$  to  $E_i(s)$  for the network shown in figure (1).



(7M+8M)

Figure (1)

2. a) Derive the transfer function for AC servomotor.  
b) Obtain the overall transfer function  $C(s)/R(s)$  of the system shown in figure 2 using block diagram reduction technique. Draw the signal flow graph for the same system and verify the result by using Mason's formula. (8M+7M)

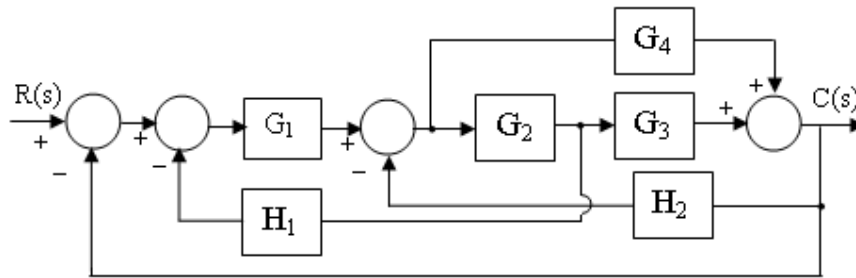
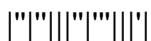


Figure 2

3. a) Sketch the unit step response of a prototype second order system and show that the percentage over shoot is a function of a damping factor alone.  
b) For a unity feedback system the open loop transfer function is given by

$$G(s) = \frac{200}{s(s+10)}$$

Determine: i) maximum overshoot ii) rise time iii) settling time and iv) steady state error if the input is a unit step. (7M+8M)



4. a) Open loop transfer function of a unity feedback system is

$$G(s) = \frac{K}{(s+1)(s+3)(s^2+6s+25)}$$

By applying Routh Criterion, determine the values of K which will cause sustained oscillations in the closed-loop system. What are the corresponding oscillations of frequency?

- b) Sketch the root locus diagram for the unity feedback system having open loop transfer function

$$G(s) = \frac{K}{s(s+4)(s^2+4s+20)} \quad (7M+8M)$$

5. Draw Bode plots for  $G(s)H(s) = \frac{70}{s(0.25s+1)(0.1s+1)}$ .

Determine gain margin and phase margin from these plots. (15M)

6. The open loop transfer function of a unity feedback control system is  $G(s) = \frac{K}{(s+1)(2s+1)}$ .

Use Nyquist stability criterion to determine the critical value of gain 'K' for stability. (15M)

7. a) Draw electrical network configuration for phase-lag compensator and hence derive the transfer function for the same.

b) Explain the procedural steps to design a phase lead compensator using Bode analysis.

(7M+8M)

8. a) What do you understand by state transition matrix? State and prove its properties.

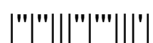
b) Determine the time response of the following system

$$\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \end{bmatrix} = \begin{bmatrix} 0 & 1 \\ -6 & -5 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} + \begin{bmatrix} 0 \\ 1 \end{bmatrix} u(t)$$

$$y(t) = [1 \quad 0] \begin{bmatrix} x_1 \\ x_2 \end{bmatrix}$$

Where  $u(t)$  is the unit step input and  $x_1(0) = x_2(0) = 0$ .

(8M+7M)



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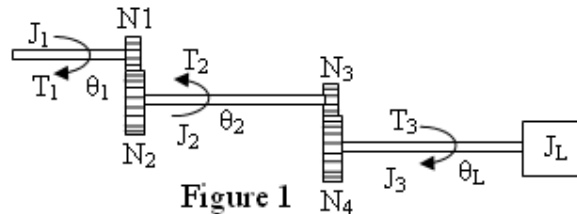
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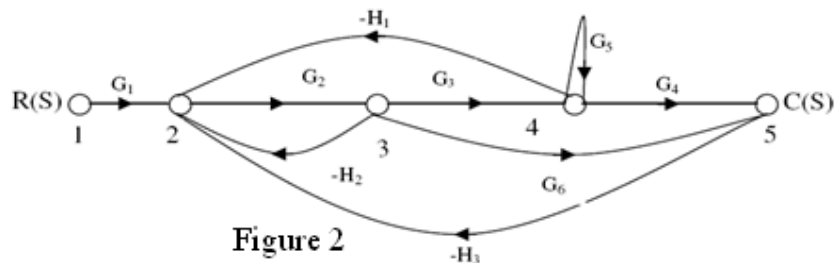
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Answer any **FIVE** Questions  
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1. a) What is the classification of control systems and discuss the importance of mathematical modeling of a control system.
- b) For the geared system shown below in Figure 1, find the transfer function relating the angular displacement  $\theta_L$  to the input torque  $T_1$ , where  $J_1, J_2, J_3$  refer to the inertia of the gears and corresponding shafts.  $N_1, N_2, N_3,$  and  $N_4$  refer to the number of teeth on each gear wheel. (7M+8M)



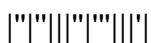
2. a) Explain the working of Synchro transmitter and receiver.
- b) For the system illustrated by the signal flow graph shown in Figure 2, obtain the overall transfer function by means of Mason's formula. (8M+7M)



3. a) Illustrate the effects of proportional derivative control on transient performance of feedback control systems.
- b) For a unity feedback control system the open loop transfer function is given by

$$G(s) = \frac{10}{s(s+4)}$$

Determine damping ratio, natural un-damped resonance frequency, percentage peak overshoot and an expression for error response for a unit step input function. (8M+7M)



4. a) For the system whose characteristic equation is given by

$$F(s) = s(s+5)(s+6)(s^2 + 4s + 25) + K(s+3) = 0,$$

Determine the values of K which will cause sustained oscillations in the closed-loop system using Routh Criterion. What are the corresponding oscillations of frequency?

- b) Sketch the root locus for the unity feedback system having open loop transfer function

$$G(s) = \frac{K}{s(s+4)(s^2 + 4s + 40)}. \quad (7M+8M)$$

5. The open loop transfer function of a unity feedback control system is given by

$$G(s) = \frac{K}{s(1+0.2s)(1+0.02s)}.$$

Draw Bode plots in magnitude and phase and hence determine the following:

- Gain margin when  $K = 1$ .
  - The value of K for gain margin to be 20 dB.
  - The phase margin corresponding to the above value of K.
  - Gain margin, phase margin and corresponding frequencies for  $K = 10$ . (15M)
6. Using Nyquist criterion determine condition for stability for the unity feedback system having open loop transfer function

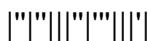
$$G(s) = \frac{K}{s(1+\tau_1s)(1+\tau_2s)}. \quad (15M)$$

7. a) Draw electrical network configuration for phase lag-lead compensator and hence derive the transfer function for the same.
- b) Explain the design procedure for lag-lead compensation in frequency domain. (7M+8M)

8. a) Define the term state variable. What are the advantages of state space representation?
- b) Find the transfer function of the system whose state space representation is given by

$$\dot{x} = Ax + Bu, \quad y = Cx \quad \text{with}$$

$$A = \begin{bmatrix} -1 & -4 & -1 \\ -1 & -6 & -2 \\ -1 & -2 & -3 \end{bmatrix}, \quad B = \begin{bmatrix} 0 \\ 1 \\ 1 \end{bmatrix} \quad \text{and} \quad C = [1 \quad 1 \quad 1] \quad (6M+9M)$$



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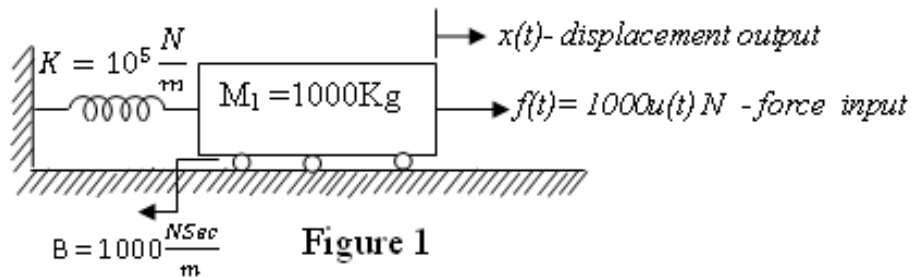
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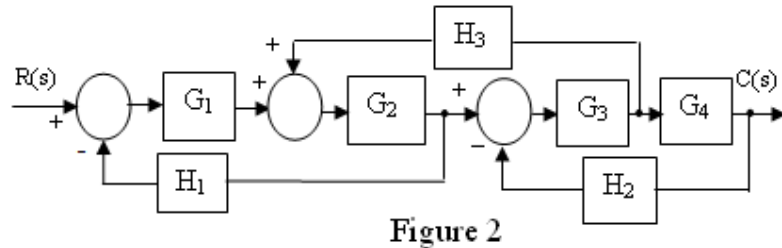
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1. a) Define the transfer function and discuss the limitations in transfer function representation.  
b) Write the differential equations for the Mechanical system shown in Figure 1. Determine the transfer function (7M+8M)



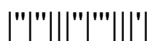
2. a) Derive the transfer function of field controlled dc servomotor.  
b) Obtain overall transfer function  $C(s)/R(s)$  of the system shown in figure 2 using block diagram reduction technique. Draw the signal flow graph for the same system and verify the result using Mason's gain formula. (7M+8M)



3. a) Illustrate the effect of the value of damping ratio on the location of closed-loop poles of a standard second order system.  
b) The open loop transfer function of a control system with unity feedback is

$$G(s) = \frac{500}{s(1 + 0.1s)}$$

Evaluate the error series for the system and determine the steady state error of the system when an input of  $r(t) = 1 + 2t + t^2; t > 0$  is applied. (6M+9M)



4. a) Briefly explain about Routh-Hurwitz criterion.

b) A feedback control system has loop transfer function  $G(s)H(s) = \frac{K}{s(s+2)(s+10)}$ .

Sketch the root locus and determine the range of 'K' for which the system is stable.

(6M+9M)

5. A unity feedback control system has forward path transfer function as  $G(s) = \frac{36}{(s+1)(s+3)^2}$ .

Construct Bode plots and find the following:

i) Gain crossover and phase crossover frequencies.

ii) Gain margin and phase margin.

(15M)

6. Plot the Nyquist plot for  $G(s)H(s) = \frac{K(s-1)}{s(s+1)}$ .

For  $K > 0$  find the number of closed loop poles in the right half s-plane and comment on stability.

(15M)

7. a) Design a lag compensator that will provide a phase lag of  $50^\circ$  and alternation of 15 dB at 2 rad/sec. Also determine the transfer function

b) Write the transfer function of a lag compensator and draw its pole zero and frequency response plots.

(7M+8M)

8. a) Explain the concept of state, state variables and state model.

b) Find  $x_1(t)$  and  $x_2(t)$  of the system described by  $\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \end{bmatrix} = \begin{bmatrix} 0 & 1 \\ -3 & -2 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix}$  where the initial

conditions are  $x_1(0) = 1$  and  $x_2(0) = -1$ .

(7M+8M)

