

IV B.Tech II Semester Regular Examinations, April/May - 2014

DIGITAL CONTROL SYSTEMS

(Electrical and Electronics Engineering)

Time : 3 hours

Max. Marks: 75

Answer any Five Questions
All Questions carry equal marks

- 1 a) Explain about the shifting and scaling operator. [8]
b) Discuss briefly about the linear time invariant and causal systems. [7]
- 2 a) Write the mapping points between S-Plane and Z-plane. [7]
b) Find the z-transform of (i) unit step (ii) $f(t) = t e^{-at}$ [8]
- 3 a) Explain about the weighted resistor 3 bit D/A converter? [7]
b) Explain any examples of data control systems? [8]
- 4 a) What are the methods for computation of state transition matrix. Explain any one method? [7]
b) A discrete time system is described by the differential equation $y(k + 2) + 5y(k + 1) + 6y(k) = 4U(k)$ assuming initial conditions are $y(0) = 1, y(1) = 0, T = 1$ sec. Find the state transition matrix. [8]
- 5 a) Explain the Duality between controllability and observability. [7]
b) Consider that a digital control system is described by the state equation. [8]
 $x(k + 1) = Ax(k) + Bu(k)$
Where
 $A = \begin{bmatrix} 1 & -2 & 0 \\ 3 & 2 & 1 \\ -1 & 1 & 4 \end{bmatrix}, B = \begin{bmatrix} 1 & 0 \\ -1 & 1 \\ 0 & 1 \end{bmatrix}$, Determine the controllability of the system.
- 6 a) Explain the following mapping between the S-Plane and the Z-Plane. [12]
(i) Primary strips and complementary Strips (ii) Constant frequency loci
(iii) Constant damping ratio loci
b) Explain the stability conditions of closed loop systems in the Z over in the S-plane. [3]
- 7 a) Write the transient response specifications? [7]
b) Explain the design procedure in the w-plane? [8]
- 8 a) Discuss the necessary conditions for design of state feedback controller through pole placement? [10]
b) Explain about the state observers? [5]

Code No: R42021

R10

Set No. 2

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- 1 Explain in detail about the periodic and nonperiodic signals with a neat sketch? [15]
- 2 a) Solve the following difference equation [5]
 $y(k + 2) + 3y(k + 1) + 2y(k) = 0; y(-1) = -\frac{1}{2}, y(-2) = \frac{3}{4}$
b) Obtain the z transform of $f(t) = e^{-at}$ [5]
c) Find the inverse z-transform of $F(Z) = \frac{1}{z(z-0.2)}$ [5]
- 3 a) State and prove the sampling theorem? [7]
b) Derive transfer functions for the following data hold circuits. [8]
(i) Zero order hold circuit (ii) First order hold circuit
- 4 a) Write the controllable and diagonal canonical forms? [7]
b) Consider a discrete linear data control system, whose input-output relation is described by the difference equation $y(k + 2) + 2y(k + 1) + y(k) = u(k)$ initial conditions are $x(0) = 0$ and $x(1) = 1$. Test the state controllable and observable canonical forms? [8]
- 5 a) Explain the concepts of controllability and observability. [7]
b) Investigate the controllability and observability of the digital system. [8]
 $x(k + 1) = \begin{bmatrix} -1 & 1 \\ 0 & -1 \end{bmatrix} x(k) + \begin{bmatrix} 0 \\ 1 \end{bmatrix} u(k)$ and $y(k) = [1 \quad 1]x(k)$
- 6 a) List the difference between the Jury stability test and stability analysis using bilinear transformation coupled with routh stability criterion? [7]
b) Consider the discrete time unity feedback control system (T=1 sec) whose open loop pulse transfer function is given by [8]
$$G(z) = \frac{K(0.3679Z + 0.2642)}{(Z - 0.3679)(Z - 1)}$$
Determine the range of K for stability by use of the Jury stability test.
- 7 a) Discuss about the response of a linear time invariant discrete time system to a sinusoidal input? [7]
b) Consider the system defined by $x(kT) = u(kT) + ax((k - 1)T)$, $0 < a < 1$ [8]
Where $u(kT)$ is the input and $x(kT)$ the output. Obtain the steady state output $x(kT)$, when the input $u(kT)$ is the sampled sinusoidal.
- 8 Derive the necessary and sufficient conditions for design of state feedback controller through pole placement? [15]

Answer any Five Questions**All Questions carry equal marks**

- 1 Discuss in detail about the continuous and discrete time signals with neat sketches? [15]
- 2 a) Obtain the Z-transform of the following [8]
 (i) $x(t) = \frac{1}{a}(1 - e^{-at})$ (ii) $x(t) = t^2 e^{-at}$ where 'a' is constant
- b) Consider $x(z)$ where $x(z) = \frac{2z^3 + z}{(z-2)^2(z-1)}$ obtain the inverse Z-transform of $x(z)$. [7]
- 3 a) What are the various types of analog to digital converters? Explain successive approximation type analog to digital converters with neat schematic diagram? [8]
 b) Describe the sample and hold operations? [7]
- 4 a) Write the state transition matrix and its properties? [7]
 b) Obtain the state transition matrix of the following discrete time system [8]
 $x(k+1) = Gx(k) + Hu(k)$
 $y(k) = Cx(k)$
 Where
 $G = \begin{bmatrix} 0 & 1 \\ -2 & -2 \end{bmatrix}, H = \begin{bmatrix} 1 \\ 1 \end{bmatrix}, C = [1 \quad 0]$
- 5 a) Explain the test for controllability and observability. [7]
 b) Given the system [8]
 $x(k+1) = Ax(k) + Bu(k)$
 $y(k) = c x(k)$
 Where $A = \begin{bmatrix} 0 & 1 \\ -1 & -3 \end{bmatrix}, B = \begin{bmatrix} 1 \\ 2 \end{bmatrix}, C = [1 \quad 1]$
 Determine the state controllability of the system.
- 6 a) State and explain the jury stability test. [8]
 b) Using Jury's stability criterion find the range of K, for which the characteristic equation $z^3 + Kz^2 + 1.5Kz - (K+1) = 0$ is closed loop stable. [7]
- 7 a) Explain the relation between the bilinear transformation and the w plane? [7]
 b) Discuss the review of phase lag, lead and lag-lead compensator? [8]
- 8 a) Explain the sufficient conditions for design of state feedback controller through pole placement? [7]
 b) Derive the ackerman's formula? [8]

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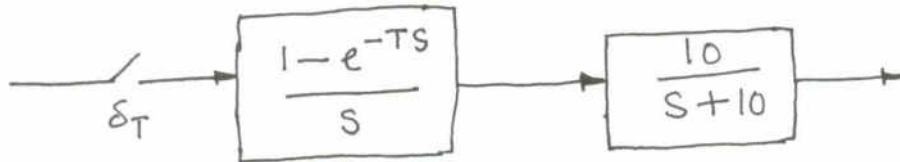
- 1 a) Explain about the discrete time signals with a neat sketch? [8]
 b) Describe about the nonperiodic signals with a neat sketch? [7]
- 2 a) State and prove the following Z-Transform theorems [7]
 (i) Shifting theorem (left & right) (ii) Initial value theorem
 (iii) Final value theorem
 b) Find the Z-transform of the following [8]
 (i) $f(t) = e^{-at} \sin \omega t$ (ii) $f(s) = \frac{4}{s^2(s+2)}$
- 3 a) What are the advantages of sampling process in control systems? [5]
 b) Explain any two types of digital to analog converters with a neat circuit? [10]
- 4 a) What are the state space representation forms and explain them. [8]
 b) Consider the following system. [7]

$$\frac{Y(z)}{U(z)} = \frac{Z+1}{Z^2+1.3Z+0.4}$$
 Obtain the state space representation forms of controllable and observable canonical forms.
- 5 a) Derive the necessary condition for the digital control system [7]
 $X(K+1) = AX(K)+Bu(K)$
 $C(k) = DX(K)$ to be observable.
 b) Examine whether the discrete data system [8]

$$x(k+1) = \begin{bmatrix} 0 & 1 \\ -2 & -2 \end{bmatrix} x(k) + \begin{bmatrix} 1 \\ -1 \end{bmatrix} u(k)$$

$$y(k) = [1 \ 0]x(k)$$
 Is (i) state controllable (ii) output controllable and (iii) observable.
- 6 a) Discuss the stability analysis of discrete control system using (i) Routh stability [7]
 criteria (ii) Bilinear transformation
 b) Using Jury's stability criterion, determine the stability of the following discrete [8]
 time systems
 (i) $z^3 + 3.3z^2 + 4z + 0.8 = 0$ (ii) $z^3 - 1.1z^2 - 0.1z + 0.2 = 0$

- 7 a) Explain about the digital PID controllers with neat sketch? [10]
- b) Consider the transfer function system shown. The sampling period T is assumed to be 0.1 sec. obtain $G(w)$.



- 8 a) Explain the concept of state feedback controllers? [5]
- b) Consider the system $x(k + 1) = Gx(k) + Hu(k)$ [5]
- $$G = \begin{bmatrix} 0 & 1 \\ -0.16 & -1 \end{bmatrix}, H = \begin{bmatrix} 0 \\ 1 \end{bmatrix}$$
- Determine a suitable state feedback gain matrix 'k' such that the system will have the closed loop poles at $z = 0.5 \pm j0.5$

[10]